

# The GH-Method

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## **Viscoelastic Glucose Theory (VGT #6): Applying Viscoelastic Glucose Theory with Fasting Plasma Glucose (FPG) as the Strain Along with the FPG Change Rate Multiplied by Body Temperature in the Early Morning as the Stress, to Illustrate the Viscoelastic Stress-Strain Diagram and Calculate the Predicted FPG Values Using the Perturbation Theory Model and Amplified Body Temperature Ratio as the “Perturbation Factor”, then Comparing Against the Predicted FPG Values Using Statistical Linear Regression Model Based on GH-Method: Math-Physical Medicine (No. 583)**

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**Note:** Readers who want to get a quick overview can read the abstract, results, and graphs.

### **Abstract**

The author has studied strength of materials and theory of elasticity through his undergraduate courses at the University of Iowa. He also conducted research work to earn a master's degree in Biomechanics under Professor James Andrews. At that time, he used the spring and dashpot models to simulate the behaviors of human joints, bones, muscles, and tendons in order to investigate the human-weapon interactions during the Vietnam war era. Later, he went to MIT to pursue his PhD study under Professor Norman Jones, who taught him theory of plasticity and dynamic plastic behaviors of various structure elements. He also took additional graduate courses in the field of fluid dynamics and thermodynamics. Since then, many advancements have been made in the biomechanics branch, especially with human body tissues that possess certain viscoelastic characteristics, such as bones, muscles, cartilages, tendons (connect bone to muscle), ligaments (connect bone to bone), fascia, and skin. For example, the author suffered plantar fasciitis for many years. He understood that the night splint dorsiflexes forefoot, at the back of the foot, increases plantar fascia tension to offer stress-relaxation for the pain. This model of muscles and tendons connecting the lower leg and foot is a form of viscoelastic study for medical problem solving. However, when dealing with human internal organs, it is not easy to conduct live experiments to obtain accurate measurements

for the biomedical material properties. Although blood itself is a viscous material (time-dependent), its viscosity factor may fall between water, honey, syrup, or gel. But the author's research subject is “glucose” where the blood sugar amount is produced by the liver and also carried by red blood cells, not the blood itself. Fasting plasma glucose (FPG) has nothing to do with either diet or exercise during sleep hours and is mainly relying on the pancreatic beta cell's health condition, which produces and releases insulin, to control the glucose level in blood. Therefore, it is nearly impossible to measure material geometry or certain engineering properties of glucose, for example, to determine the viscosity of “glucose”. Therefore, the best he could do is to apply the “concept of viscoelasticity and/or viscoplasticity” to construct an analogy model of time-dependent glucose behaviors. The author's background includes mathematics, physics, and various engineering disciplines, not including biology and chemistry. As a result, he can only investigate the observed biomedical phenomena using his ready-learned math-physical tools. He studied both modern physics and quantum mechanics during his school days. Therefore, he applied the theory of relativity on interactions among the human organs in the human body (inner space) which is similar to the inter-relationships among the planets in the universe (outer space). He utilized the perturbation theory to obtain an approximate but accurate enough predicted glucose level along

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with the estimation for the associated energy of glucose. In addition, he conducted some investigations of glucose behaviors using elasticity theory and plasticity theory, which allowed him to write a few articles on his research findings. In this viscoelasticity study, he utilized the average FPG value of sleep time over 7 hours as the strain along with the body temperature measured in the early morning as the stress. In a recent email from Professor Norman Jones, he said that: "I have wondered if the use of viscoelastic/viscoplastic materials might be of some value to your studies. These phenomena embrace time-dependent behaviour and I know that you have emphasized the time-dependence of various behaviours in the body. Just a thought." His suggestion triggered the author's strong interest and desire to research this subject of glucose behaviors further by using the viscosity theory. This article is a follow-up to his previous 5 papers. Paper No. 578 focused on certain generic characteristics of viscoelastic glucose behaviors. Paper No. 579 concentrated on the comparison via stress-strain diagrams between viscoelastic glucose versus viscoplastic glucose. Paper No. 580 explored certain similarity and difference of stress-strain diagrams resulting from his postprandial plasma glucose (PPG) over the past 3.7 years and Y2021 using the viscoelasticity theory. Paper No. 581 studied the differences of engineering illustrations for three publicly available PPG waveforms for normal people, pre-diabetes patients, and severe diabetes patients. Paper No. 582, he used a set of his collected continuous glucose monitoring (CGM) sensor PPG data and waveforms and separated them into three glucose levels, < 140 mg/dL (pre-diabetes from 4,122 meals), 140-170 mg/dL (diabetes from 119 meals), and > 170 mg/dL (severe diabetes from 37 meals). He conducted his glucose stress-strain behavior analyses and to identify which glucose level matches with a state of linear elastic, plastic, viscoelastic, or viscoplastic. In this article, he focused on the FPG domain which has nothing to do with either food or exercise. In his earlier research work, he has identified FPG having a high degree of correlation (~90% or higher) with body weight or body temperature measured in the early morning. Here, he has chosen the body temperature as the sole input which influences his FPG level as the output. As a result, he applied three different analysis models of viscoelasticity, perturbation, and statistical regression. The author utilizes his own FPG value as the strain ( $\epsilon$ ) and the respective strain rate of  $(d\epsilon/dt)/30$  multiplied with the viscosity factor ( $\eta$ ) as the stress. Since it is difficult for him to determine the viscosity factor ( $\eta$ ) of FPG, he makes a bold assumption by using his body temperature of present time as his viscosity factors. These described assumptions have lead into the following defined stress and strain equations: Stress  $\sigma = \eta * (d\epsilon/dt)/30 = (\text{viscosity factor of body temperature at present month}) * (\text{present FPG} - \text{previous FPG})/30$ . Strain  $\epsilon =$

(individual FPG at present month). To offer a simple explanation to readers who do not have a physics or engineering background, the author includes a brief excerpt from Wikipedia regarding the description of basic concepts for elasticity and plasticity theories, viscoelasticity and viscoplasticity theories from the disciplines of engineering and physics in the Method section. The analogy between physics and medicine is twofold. First, the force or stress ( $\sigma$ ) in physics and engineering (y-axis) corresponds to the influential force or load on our body for pushing FPG upward or downward in medicine, e.g. body temperature or body weight. Second, the deformation or strain ( $\epsilon$ ) in physics and engineering (x-axis) corresponds to the actual FPG level in medicine. The first influential factor is the "strain rate", i.e. "the change amount of FPG in a certain amount of time duration". In this study, the time duration is 30 since his selected time periods are monthly. The second influential factor of stress is the selection of viscosity factors ( $\eta$ ) which is  $(\text{present body temperature} / \text{previous body temperature}) * \text{amplification factor of 5}$ . The reason for inserting an amplification factor is due to the body temperature's fluctuation range being within a narrow range of 97.0 to 98.0 degree Fahrenheit. Therefore, the body temperature change rate signal must be amplified in order to serve its useful role as a perturbation factor. Nevertheless, the medical field is quite different from the engineering field, where the engineering materials such as steel, copper, concrete, and aluminum are inorganic in most cases. These material properties do not change significantly over their expected lifespans. However, in medicine, the body with its organs and cells are organic and go through many distinct stages over their natural lifespans, such as birth, splitting, growth, mutation, development, repair, sickness, and death. Therefore, the biomedical properties are "moving targets" which vary with the individual person, severity of diabetes, and selected different time-windows. In other words, they are both time-dependent and specimen-dependent, because these fundamental characteristics, calculations of cross-section of subject, bending moment of resistance, or the shape-factors in solid mechanics are not applicable in this biomedical glucose analogy study of elasticity/plasticity or viscoelasticity/viscoplasticity. The most important part, in the author's opinion, is that by applying the concept of elasticity/plasticity theory or viscoelasticity/viscoplasticity theory on understanding or illustrating the observed biomedical phenomena is extremely useful to explore deep insights or enable the prediction of glucoses, particularly for both hyperglycemic conditions (leading into various internal organ complications) and hypoglycemic conditions (insulin shock leading to possible sudden death). In conclusion, he defines his stress-strain equations as follows: strain =  $\epsilon = \text{individual FPG value at present month}$ . Stress =  $\sigma = \eta * (d\epsilon/dt) =$

$\eta * (d\text{-strain}/d\text{-time}) = (\text{viscosity factor using body temperature at month}) * (\text{present FPG} - \text{previous FPG}) / 30$ , where 30 indicates the 30-days timespan of his collected monthly data. Based on viscoelasticity theory, perturbation theory, and statistical linear regression model, the following 3 distinct observations are evident: (1) From time-domain analysis, the correlation between FPG and body temperature is 71%. However, the body temperature's fluctuation range is narrow, within 97 to 98 degrees Fahrenheit. Therefore, an amplification factor of 5 was chosen to amplify the influence of body temperature for the predicted FPG values. (2) From stress-strain diagram of using FPG as the strain versus  $(d\text{-FPG}/dt) * \text{body temperature}$  as the stress, an enclosed hysteresis loop indicates that this stress-strain relationship is viscoelastic, i.e. FPG returning to the beginning

position and also time-dependent. (3) From the comparison of the 3 sets of FPG values: measured FPG, perturbed FPG, and regression FPG, both of the perturbed FPG and regression FPG have achieved 100% of prediction accuracy. On residence of correlations, measured vs. perturbed has a 71% correlation, measured vs. regression has a 70% correlation, while perturbed vs. regression has a 50% correlation. All 3 correlations are "statistically significant". In summary, from a daily practice viewpoint, using body temperature as the input and applying the combination of viscoelasticity theory of engineering and perturbation theory of quantum mechanics, or applying the linear regression analysis model of statistics, both of these 2 final predicted FPG results are satisfactory.

**Keywords:** Viscoelastic; Fasting plasma glucose; Diabetes; Glucose

**Abbreviations:** FPG: fasting plasma glucose; CGM: continuous glucose monitoring

## 1. INTRODUCTION

The author has studied strength of materials and theory of elasticity through his undergraduate courses at the University of Iowa. He also conducted research work to earn a master's degree in Biomechanics under Professor James Andrews. At that time, he used the spring and dashpot models to simulate the behaviors of human joints, bones, muscles, and tendons in order to investigate the human-weapon interactions during the Vietnam war era. Later, he went to MIT to pursue his PhD study under Professor Norman Jones, who taught him theory of plasticity and dynamic plastic behaviors of various structure elements. He also took additional graduate courses in the field of fluid dynamics and thermodynamics.

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In a recent email from Professor Norman Jones, he said that: "I have wondered if the use of viscoelastic/viscoplastic materials might be of some value to your studies. These phenomena embrace time-dependent behaviour and I know that you have emphasized the time-dependence of various behaviours in the body. Just a thought." His suggestion triggered the author's strong interest and desire to research this subject of glucose behaviors further by using the viscosity theory. This article is a follow-up to his previous 5 papers. Paper No. 578 focused on certain generic characteristics of viscoelastic glucose behaviors. Paper No. 579 concentrated on the comparison via stress-strain diagrams between viscoelastic glucose versus viscoplastic glucose. Paper No. 580 explored certain similarity and difference of stress-strain diagrams resulting from his postprandial plasma glucose (PPG) over the past 3.7 years and Y2021 using the viscoelasticity theory. Paper No. 581 studied the differences of engineering illustrations for three publicly available PPG waveforms for normal people, pre-diabetes patients, and severe diabetes patients. Paper No. 582, he

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The author utilizes his own FPG value as the strain ( $\epsilon$ ) and the respective strain rate of  $(d\epsilon/dt)/30$  multiplied with the viscosity factor ( $\eta$ ) as the stress. Since it is difficult for him to determine the viscosity factor ( $\eta$ ) of FPG, he makes a bold assumption by using his body temperature of present time as his viscosity factors.

These described assumptions have lead into the following defined stress and strain equations:

$$\begin{aligned} \text{Stress } \sigma &= \eta * (d\epsilon/dt)/30 \\ &= (\text{viscosity factor of body temperature at present month}) * (\text{present FPG} - \text{previous FPG})/30 \end{aligned}$$

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of glucoses, particularly for both hyperglycemic conditions (leading into various internal organ complications) and hypoglycemic conditions (insulin shock leading to possible sudden death).

## 2. METHODS

### 2.1 Elasticity, plasticity, viscoelasticity, and viscoplasticity

The difference between elastic materials and viscoelastic materials (from “Soborthans, innovating shock and vibration solutions”).

What are elastic materials?

Elasticity is the tendency of solid materials to return to their original shape after forces are applied on them. When the forces are removed, the object will return to its initial shape and size if the material is elastic.

What are viscous materials?

Viscosity is a measure of a fluid’s resistance to flow. A fluid with large viscosity resists motion. A fluid with low viscosity flows. For example, water flows more easily than syrup because it has a lower viscosity. High viscosity materials might include honey, syrups, or gels – generally things that resist flow. Water is a low viscosity material, as it flows readily. Viscous materials are thick or sticky or adhesive. Since heating reduces viscosity, these materials don't flow easily. For example, warm syrup flows more easily than cold.

What is viscoelastic?

Viscoelasticity is the property of materials that exhibit both viscous and elastic characteristics when undergoing deformation. Synthetic polymers, wood, and human tissue, as well as metals at high temperature, display significant viscoelastic effects. In some applications, even a small viscoelastic response can be significant.

Elastic behavior versus viscoelastic behavior

The difference between elastic materials and viscoelastic materials is that viscoelastic materials have a viscosity factor and the elastic ones don't. Because viscoelastic materials have the viscosity factor, they have a strain rate dependent on time. Purely

elastic materials do not dissipate energy (heat) when a load is applied, then removed; however, a viscoelastic substance does.

The following brief introductions are excerpts from Wikipedia:

“Elasticity (physics):

Physical property when materials or objects return to original shape after deformation.

In physics and materials science, elasticity is the ability of a body to resist a distorting influence and to return to its original size and shape when that influence or force is removed. Solid objects will deform when adequate loads are applied to them; if the material is elastic, the object will return to its initial shape and size after removal. This is in contrast to plasticity, in which the object fails to do so and instead remains in its deformed state.

The physical reasons for elastic behavior can be quite different for different materials. In metals, the atomic lattice changes size and shape when forces are applied (energy is added to the system). When forces are removed, the lattice goes back to the original lower energy state. For rubbers and other polymers, elasticity is caused by the stretching of polymer chains when forces are applied.

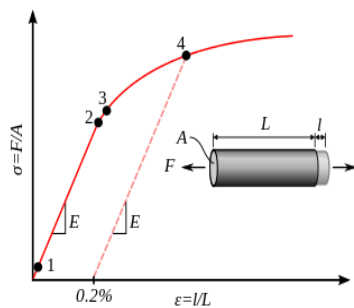
Hooke's law states that the force required to deform elastic objects should be directly proportional to the distance of deformation, regardless of how large that distance becomes. This is known as perfect elasticity, in which a given object will return to its original shape no matter how strongly it is deformed. This is an ideal concept only; most materials which possess elasticity in practice remain purely elastic only up to very small deformations, after which plastic (permanent) deformation occurs.

In engineering, the elasticity of a material is quantified by the elastic modulus such as the Young's modulus, bulk modulus or shear modulus which measure the amount of stress needed to achieve a unit of strain; a higher modulus indicates that the material is harder to deform. The material's elastic limit or yield strength is the maximum stress that can arise before the onset of plastic deformation.

Plasticity (physics):

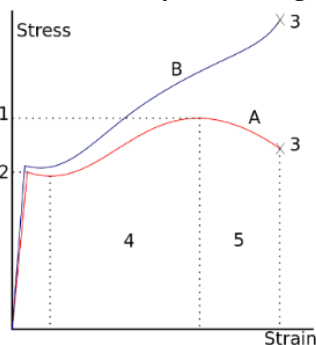
Deformation of a solid material undergoing non-reversible changes of shape in response to applied forces.

In physics and materials science, plasticity, also known as plastic deformation, is the ability of a solid material to undergo permanent deformation, a non-reversible change of shape in response to applied forces. For example, a solid piece of metal being bent or pounded into a new shape displays plasticity as permanent changes occur within the material itself. In engineering, the transition from elastic behavior to plastic behavior is known as yielding.



A stress-strain curve showing typical yield behavior for nonferrous alloys.

1. True elastic limit
2. Proportionality limit
3. Elastic limit
4. Offset yield strength



A stress-strain curve typical of structural steel.

- 1: Ultimate strength
- 2: Yield strength (yield point)
- 3: Rupture
- 4: Strain hardening region
- 5: Necking region
- A: Apparent stress (F/A0)
- B: Actual stress (F/A)

Plastic deformation is observed in most materials, particularly metals, soils, rocks, concrete, and foams. However, the physical mechanisms that cause plastic deformation can vary widely. At a crystalline scale, plasticity in metals is usually a consequence of dislocations. Such defects are relatively rare in most crystalline materials, but are numerous in some and part of their crystal structure; in such cases, plastic crystallinity can result. In brittle materials such as rock, concrete and bone, plasticity is caused predominantly by slip at microcracks. In cellular materials such as liquid foams or biological tissues, plasticity is mainly a consequence of bubble or cell rearrangements, notably T1 processes.

For many ductile metals, tensile loading applied to a sample will cause it to behave in an elastic manner. Each increment of load is accompanied by a proportional increment in extension. When the load is removed, the piece returns to its original size. However, once the load exceeds a threshold – the yield strength – the extension increases more rapidly than in the elastic region; now when the load is removed, some degree of extension will remain.

Elastic deformation, however, is an approximation and its quality depends on the time frame considered and loading speed. If, as indicated in the graph opposite, the deformation includes elastic deformation, it is also often referred to as "elasto-plastic deformation" or "elastic-plastic deformation".

Perfect plasticity is a property of materials to undergo irreversible deformation without any increase in stresses or loads. Plastic materials that have been hardened by prior deformation, such as cold forming, may need increasingly higher stresses to deform further. Generally, plastic deformation is also dependent on the deformation speed, i.e. higher stresses usually have to be applied to increase the rate of deformation. Such materials are said to deform viscoplastically.”

Viscoelasticity:

Property of materials with both viscous and elastic characteristics under deformation.

In materials science and continuum mechanics, viscoelasticity is the property of

materials that exhibit both viscous and elastic characteristics when undergoing deformation. Viscous materials, like water, resist shear flow and strain linearly with time when a stress is applied. Elastic materials strain when stretched and immediately return to their original state once the stress is removed.

Viscoelastic materials have elements of both of these properties and, as such, exhibit time-dependent strain. Whereas elasticity is usually the result of bond stretching along crystallographic planes in an ordered solid, viscosity is the result of the diffusion of atoms or molecules inside an amorphous material.

In the nineteenth century, physicists such as Maxwell, Boltzmann, and Kelvin researched and experimented with creep and recovery of glasses, metals, and rubbers. Viscoelasticity was further examined in the late twentieth century when synthetic polymers were engineered and used in a variety of applications. Viscoelasticity calculations depend heavily on the viscosity variable,  $\eta$ . The inverse of  $\eta$  is also known as fluidity,  $\phi$ . The value of either can be derived as a function of temperature or as a given value (i.e. for a dashpot).

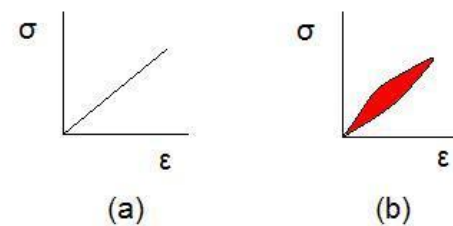
Depending on the change of strain rate versus stress inside a material, the viscosity can be categorized as having a linear, non-linear, or plastic response. When a material exhibits a linear response it is categorized as a Newtonian material. In this case the stress is linearly proportional to the strain rate. If the material exhibits a non-linear response to the strain rate, it is categorized as Non-Newtonian fluid. There is also an interesting case where the viscosity decreases as the shear/strain rate remains constant. A material which exhibits this type of behavior is known as thixotropic. In addition, when the stress is independent of this strain rate, the material exhibits plastic deformation. Many viscoelastic materials exhibit rubber like behavior explained by the thermodynamic theory of polymer elasticity.

Cracking occurs when the strain is applied quickly and outside of the elastic limit. Ligaments and tendons are viscoelastic, so the extent of the potential damage to them depends both on the rate of the change of their length as well as on the force applied.

A viscoelastic material has the following properties:

- hysteresis is seen in the stress-strain curve
- stress relaxation occurs: step constant strain causes decreasing stress
- creep occurs: step constant stress causes increasing strain
- its stiffness depends on the strain rate or the stress rate.

Elastic versus viscoelastic behavior:



Stress-strain curves for a purely elastic material (a) and a viscoelastic material (b). The red area is a hysteresis loop and shows the amount of energy lost (as heat) in a loading and unloading cycle. It is equal to  $\oint \sigma d\epsilon$  where  $\sigma$  is stress and  $\epsilon$  is strain.

Unlike purely elastic substances, a viscoelastic substance has an elastic component and a viscous component. The viscosity of a viscoelastic substance gives the substance a strain rate dependence on time. Purely elastic materials do not dissipate energy (heat) when a load is applied, then removed. However, a viscoelastic substance dissipates energy when a load is applied, then removed. Hysteresis is observed in the stress-strain curve, with the area of the loop being equal to the energy lost during the loading cycle. Since viscosity is the resistance to thermally activated plastic deformation, a viscous material will lose energy through a loading cycle. Plastic deformation results in lost energy, which is uncharacteristic of a purely elastic material's reaction to a loading cycle.

Specifically, viscoelasticity is a molecular rearrangement. When a stress is applied to a viscoelastic material such as a polymer, parts of the long polymer chain change positions. This movement or rearrangement is called "creep". Polymers remain a solid material even when these parts of their chains are

rearranging in order to accompany the stress, and as this occurs, it creates a back stress in the material. When the back stress is the same magnitude as the applied stress, the material no longer creeps. When the original stress is taken away, the accumulated back stresses will cause the polymer to return to its original form. The material creeps, which gives the prefix visco-, and the material fully recovers, which gives the suffix -elasticity.

#### Viscoplasticity:

Viscoplasticity is a theory in continuum mechanics that describes the rate-dependent inelastic behavior of solids. Rate-dependence in this context means that the deformation of the material depends on the rate at which loads are applied. The inelastic behavior that is the subject of viscoplasticity is plastic deformation which means that the material undergoes unrecoverable deformations when a load level is reached. Rate-dependent plasticity is important for transient plasticity calculations. The main difference between rate-independent plastic and viscoplastic material models is that the latter exhibit not only permanent deformations after the application of loads but continue to undergo a creep flow as a function of time under the influence of the applied load.

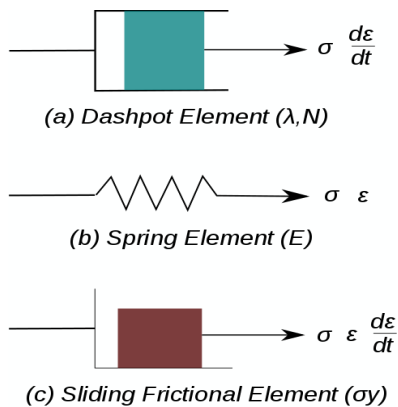


Figure 1. Elements used in one-dimensional models of viscoplastic materials.

The elastic response of viscoplastic materials can be represented in one-dimension by Hookean spring elements. Rate-dependence can be represented by nonlinear dashpot elements in a manner similar to viscoelasticity. Plasticity can be accounted for by adding sliding frictional elements as shown in Figure 1. In the figure  $E$  is the modulus of elasticity,  $\lambda$  is the viscosity

parameter and  $N$  is a power-law type parameter that represents non-linear dashpot [ $\sigma(d\epsilon/dt) = \lambda(d\epsilon/dt)^{1/N}$ ]. The sliding element can have a yield stress ( $\sigma_y$ ) that is strain rate dependent, or even constant, as shown in Figure 1c.

Viscoplasticity is usually modeled in three-dimensions using overstress models of the Perzyna or Duvaut-Lions types. In these models, the stress is allowed to increase beyond the rate-independent yield surface upon application of a load and then allowed to relax back to the yield surface over time. The yield surface is usually assumed not to be rate-dependent in such models. An alternative approach is to add a strain rate dependence to the yield stress and use the techniques of rate independent plasticity to calculate the response of a material.

For metals and alloys, viscoplasticity is the macroscopic behavior caused by a mechanism linked to the movement of dislocations in grains, with superposed effects of inter-crystalline gliding. The mechanism usually becomes dominant at temperatures greater than approximately one third of the absolute melting temperature. However, certain alloys exhibit viscoplasticity at room temperature (300K). For polymers, wood, and bitumen, the theory of viscoplasticity is required to describe behavior beyond the limit of elasticity or viscoelasticity.

In general, viscoplasticity theories are useful in areas such as

- the calculation of permanent deformations,
- the prediction of the plastic collapse of structures,
- the investigation of stability,
- crash simulations,
- systems exposed to high temperatures such as turbines in engines, e.g. a power plant,
- dynamic problems and systems exposed to high strain rates.

#### Phenomenology

For a qualitative analysis, several characteristic tests are performed to describe the phenomenology of viscoplastic materials. Some examples of these tests are

1. hardening tests at constant stress or strain rate,
2. creep tests at constant force, and
3. stress relaxation at constant elongation.

Strain hardening test

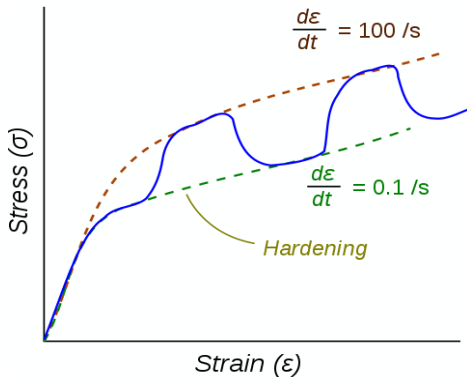


Figure 2. Stress–strain response of a viscoplastic material at different strain rates.

The dotted lines show the response if the strain-rate is held constant. The blue line shows the response when the strain rate is changed suddenly.

One consequence of yielding is that as plastic deformation proceeds, an increase in stress is required to produce additional strain. This phenomenon is known as Strain/Work hardening. For a viscoplastic material the hardening curves are not significantly different from those of rate-independent plastic material. Nevertheless, three essential differences can be observed.

1. At the same strain, the higher the rate of strain the higher the stress
2. A change in the rate of strain during the test results in an immediate change in the stress–strain curve.
3. The concept of a plastic yield limit is no longer strictly applicable.

The hypothesis of partitioning the strains by decoupling the elastic and plastic parts is still applicable where the strains are small, i.e.,

$$\epsilon = \epsilon_e + \epsilon_{vp}$$

where  $\epsilon_e$  is the elastic strain and  $\epsilon_{vp}$  is the viscoplastic strain.

To obtain the stress–strain behavior shown in blue in the figure, the material is initially

loaded at a strain rate of 0.1/s. The strain rate is then instantaneously raised to 100/s and held constant at that value for some time. At the end of that time period the strain rate is dropped instantaneously back to 0.1/s and the cycle is continued for increasing values of strain. There is clearly a lag between the strain-rate change and the stress response. This lag is modeled quite accurately by overstress models (such as the Perzyna model) but not by models of rate-independent plasticity that have a rate-dependent yield stress.

**Note:** For a more detailed description, please refer to the “consolidated method” section which is given at the beginning of the special issue.

### 3. RESULTS

Figure 1 displays the data table of both input data and calculation results.

1/24/22	Stress	Strain	Stress	Regression Analysis		Perturbation using Viscoelastic factor				
	Body Temp	FPG	(d-FPG/dt)*Temp	Month	Measured FPG	Regression FPG	Month	Measured FPG	Perturbed FPG	Regression FPG
Oct-20	97.6	93.1	0	Oct-20	93	93	Oct-20	93.1	93.1	93
Nov-20	97.9	93.1	0	Nov-20	93	104	Nov-20	93.1	93.1	104
Dec-20	97.8	103.3	33	Dec-20	103	101	Dec-20	103.3	93.1	101
Jan-21	98.0	105.7	8	Jan-21	106	107	Jan-21	105.7	105.0	107
Feb-21	98.0	111.0	17	Feb-21	111	109	Feb-21	111.0	106.1	109
Mar-21	97.9	111.0	0	Mar-21	111	105	Mar-21	111.0	111.9	105
Apr-21	97.8	107.6	-11	Apr-21	108	100	Apr-21	107.6	111.0	100
May-21	97.6	97.1	-34	May-21	97	93	May-21	97.1	107.0	93
Jun-21	97.7	101.1	13	Jun-21	101	98	Jun-21	101.1	95.4	98
Jul-21	97.7	94.0	-23	Jul-21	94	96	Jul-21	94.0	101.8	96
Aug-21	97.7	87.3	-22	Aug-21	87	97	Aug-21	87.3	92.8	97
Sep-21	97.7	93.7	21	Sep-21	94	96	Sep-21	93.7	86.2	96
Oct-21	97.7	94.6	3	Oct-21	95	96	Oct-21	94.6	94.8	96
Nov-21	97.7	94.5	0	Nov-21	95	96	Nov-21	94.5	94.7	96
Dec-21	97.6	89.9	-15	Dec-21	90	94	Dec-21	89.9	94.5	94
Jan-22	97.6	98.6	28	Jan-22	99	93	Jan-22	98.6	89.1	93
Average	97.8	98.5	1.13	Average	98.5	98.5	Average	98.5	98.1	98.5
Oct-20-Jan-22	97.8	98.4		Accuracy	100%		Accuracy	100%	Regression vs. Perturbation	
Correlation	71%			Correlation	71%		Correlation	70%	Correlation	50%
				R Square	50%		R Square	49%		
				P-Value	0.02%		Amplification	3.0		

Figure 1: Data table of both input data and calculation results.

Figure 2 shows the results from viscoelastic study. The upper diagram is the comparison of FPG and body temperature waveforms in time-domain of 16 months. The lower diagram is the stress-strain diagrams which demonstrates the viscoelastic characteristics.

Figure 3 shows the comparison of measured FPG versus two predicted FPG, via viscoelastic perturbation method and linear regression model. All of these 3 calculated correlations are high enough (50% or higher) to be considered as “statistically significant”.

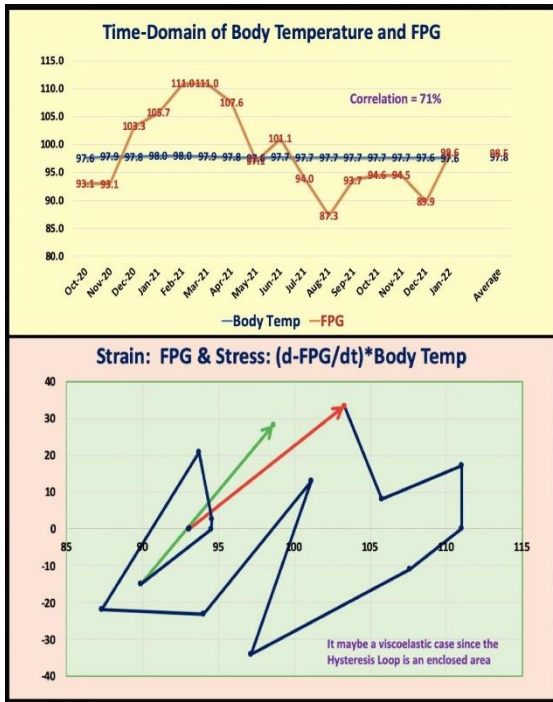


Figure 2: Time-domain FPG and body temperature (upper diagram) and viscoelastic stress-strain diagram (lower diagram).

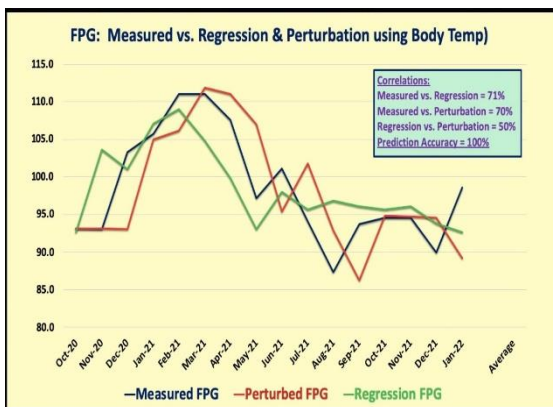


Figure 3: Comparison of measured FPG versus both viscoelastic perturbed FPG and regression FPG.

#### 4. CONCLUSION

In conclusion, he defines his stress-strain equations as follows:

Strain  
 =  $\epsilon$   
 = individual FPG value at present month

Stress  
 =  $\sigma$   
 =  $\eta * (d\epsilon/dt)$   
 =  $\eta * (d\text{-strain}/d\text{-time})$   
 = (viscosity factor using body temperature at month) \* (present FPG - previous FPG) / 30

Where 30 indicates the 30-days timespan of his collected monthly data.

Based on viscoelasticity theory, perturbation theory, and statistical linear regression model, the following 3 distinct observations are evident:

(1) From time-domain analysis, the correlation between FPG and body temperature is 71%. However, the body temperature's fluctuation range is narrow, within 97 to 98 degrees Fahrenheit. Therefore, an amplification factor of 5 was chosen to amplify the influence of body temperature for the predicted FPG values.

(2) From stress-strain diagram of using FPG as the strain versus  $(d\text{-FPG}/dt) * \text{body temperature}$  as the stress, an enclosed hysteresis loop indicates that this stress-strain relationship is viscoelastic, i.e. FPG returning to the beginning position and also time-dependent.

(3) From the comparison of the 3 sets of FPG values: measured FPG, perturbed FPG, and regression FPG, both of the perturbed FPG and regression FPG have achieved 100% of prediction accuracy. On residence of correlations, measured vs. perturbed has a 71% correlation, measured vs. regression has a 70% correlation, while perturbed vs. regression has a 50% correlation. All 3 correlations are "statistically significant".

In summary, from a daily practice viewpoint, using body temperature as the input and applying the combination of viscoelasticity theory of engineering and perturbation theory of quantum mechanics, or applying the linear regression analysis model of statistics, both of these 2 final predicted FPG results are satisfactory.

#### 5. ACKNOWLEDGMENT

Without Professor Norman Jones at MIT as his academic advisor, the author would not be able to conduct his medical research project and also published 500+ research papers. The author has never forgotten his advice to him that he should always enhance his strength on foundations, such as mathematics and physics, in order to make further improvement and advancement. Professor Jones has also provided him a personal example of doing outstanding teaching and research job with an excellent work attitude, extreme dedication, and ultimate

commitment on advancing both science and engineering.

## **6. REFERENCES**

For editing purposes, majority of the references in this paper, which are self-references, have been removed for this

article. Only references from other authors' published sources remain. The bibliography of the author's original self-references can be viewed at [www.eclairemd.com](http://www.eclairemd.com).

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# Viscoelastic and Viscoplastic Glucose Theory Application in Medicine

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